

Fundamentals of Microelectronics, 3rd Edition

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(Solution Manual)

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Chapter 1

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There are no problem sets for this chapter

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Chapter 2

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1. (a)

$$n_i(T=300\text{K}) = 1.66 \cdot 10^{15} (300)^{3/2} \cdot \exp\left[\frac{-0.66\text{eV}}{2(1.38 \cdot 10^{-23}\text{J/K})(300\text{K})}\right]$$

$$= 2.5 \cdot 10^{13} \text{ cm}^{-3}$$

$$n_i(T=600\text{K}) = 1.66 \cdot 10^{15} (600)^{3/2} \cdot \exp\left[\frac{-0.66\text{eV}}{2(1.38 \cdot 10^{-23}\text{J/K})(600\text{K})}\right]$$

$$= 4.15 \cdot 10^{16} \text{ cm}^{-3}$$

Comparing these results with those in Example:

$$\frac{n_i(\text{Ge @ } 300\text{K})}{n_i(\text{Si @ } 300\text{K})} \approx 2315.$$

$$\frac{n_i(\text{Ge @ } 600\text{K})}{n_i(\text{Si @ } 600\text{K})} \approx 27.$$

At higher temperature, the exponential terms approaches one, which implies that $n_i \sim T^{3/2}$, independent of bandgap energy, E_g .

(b) For any doped material, $n \cdot p = n_i^2$. Assuming at $T=300\text{K}$,

$$p = 5 \cdot 10^{16} \text{ cm}^{-3}$$

$$n = [n_i(T=300\text{K})]^2 / p = \frac{(2.5 \cdot 10^{13} \text{ cm}^{-3})^2}{5 \cdot 10^{16} \text{ cm}^{-3}} = 1.25 \cdot 10^{10} \text{ cm}^{-3}$$

2. (a) Mobility of electrons in Si = $1350 \text{ cm}^2/\text{V}\cdot\text{s}$
Mobility of holes in Si = $480 \text{ cm}^2/\text{V}\cdot\text{s}$

$$\Rightarrow \text{velocity of electrons} = \mu_n E = \left(1350 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}\right) \left(\frac{0.1 \text{ V}}{\mu\text{m}}\right)$$
$$= 1.35 \cdot 10^4 \text{ m/s}$$

$$\text{velocity of holes} = \mu_p E = \left(480 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}\right) \left(\frac{0.1 \text{ V}}{\mu\text{m}}\right)$$
$$= 4.8 \cdot 10^3 \text{ m/s}$$

(b) Given $E = 0.1 \text{ V}/\mu\text{m}$ hole current negligible
 $\mu_n = 1350 \text{ cm}^2/\text{V}\cdot\text{s}$ $\mu_p = 480 \text{ cm}^2/\text{V}\cdot\text{s}$

$$J_{\text{tot}} = 1 \text{ mA}/\mu\text{m}^2 = q [\mu_n n E + \mu_p p E] \approx q \mu_n n E$$

$$\therefore n = \frac{J_{\text{tot}}}{q \mu_n E} = \frac{1 \text{ mA}/\mu\text{m}^2}{(1.6 \cdot 10^{-19} \text{ C})(1350 \text{ cm}^2/\text{V}\cdot\text{s})(0.1 \text{ V}/\mu\text{m})}$$
$$= 4.6 \cdot 10^{17} \text{ cm}^{-3}$$

3. Given $L = 0.1 \mu\text{m}$ $A = (0.05 \mu\text{m})^2$ $V = 1 \text{V}$
 $\mu_n = 1350 \text{ cm}^2/\text{V-s}$ $\mu_p = 480 \text{ cm}^2/\text{V-s}$
 $n = 10^{17} \text{ cm}^{-3}$ (assuming n-type dopant)

$$(a) n_i(T=300\text{K}) = 5.2 \cdot 10^{15} (300)^{3/2} \exp\left[\frac{-1.12 \text{ eV}}{2(1.38 \cdot 10^{-23} \text{ J/K})(300\text{K})}\right]$$

$$= 1.08 \cdot 10^{10} \text{ cm}^{-3}$$

$$p = n_i^2/n = 1.17 \cdot 10^3 \text{ cm}^{-3} \quad E = V/L = 10 \text{ V}/\mu\text{m}$$

$$\therefore I_{\text{tot}} = A \cdot J_{\text{tot}} = A \cdot q [\mu_n n + \mu_p p] E$$

$$= A \cdot q [\mu_n n + \mu_p (n_i^2/n)] E$$

$$= (0.05 \mu\text{m})^2 (1.6 \cdot 10^{-19} \text{ C}) \left[\frac{1350 \text{ cm}^2}{\text{V-s}} (10^{17} \text{ cm}^{-3}) + \frac{480 \text{ cm}^2}{\text{V-s}} (1.17 \cdot 10^3 \text{ cm}^{-3}) \right]$$

$$\cdot (10 \text{ V}/\mu\text{m})$$

$$\Rightarrow I_{\text{tot}} \approx 0.054 \text{ mA}$$

$$\begin{aligned}
 \text{(b) @ 400K: } n_i &= 3.7 \cdot 10^{12} \text{ cm}^{-3} \\
 p &= n_i^2/n = 1.4 \cdot 10^8 \text{ cm}^{-3} \\
 E &= 10 \text{ V}/\mu\text{m}
 \end{aligned}$$

$$\therefore I_{\text{tot}} = A \cdot q [\mu_n n + \mu_p (n_i^2/n)] E$$

$$\begin{aligned}
 &= (0.05 \mu\text{m})^2 (1.6 \cdot 10^{-19} \text{ C}) \left[1350 \frac{\text{cm}^2}{\text{V}\cdot\text{s}} (10^{17} \text{ cm}^{-3}) + 480 \frac{\text{cm}^2}{\text{V}\cdot\text{s}} (1.4 \cdot 10^8 \text{ cm}^{-3}) \right] \\
 &\quad \cdot (10 \text{ V}/\mu\text{m})
 \end{aligned}$$

$$\Rightarrow I_{\text{tot}} \approx 0.054 \text{ mA}$$